

Muon-induced backgrounds in the CUORICINO experiment

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Abstract

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To better understand the contribution of cosmic ray muons to the CUORICINO background, ten plastic scintillator detectors were installed at the CUORICINO site and operated during the final 3 months of the experiment. From these measurements, an upper limit of 0.0021 counts/(keV·kg·yr) (95% C.L.) was obtained on the cosmic ray induced background in the neutrinoless double beta decay region of interest. The measurements were also compared to GEANT4 simulations.

Keywords: CUORICINO, muons, cosmic rays, double beta decay, neutrinos

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¹ 1. Introduction

² Understanding the nature of neutrino mass is one of the key topics at the frontier
³ of fundamental physics. One of the best opportunities for investigating this problem
⁴ is searching for neutrinoless double beta decay ($0\nu\beta\beta$), a transition in which a nucleus
⁵ (A, Z) decays into a daughter ($A, Z + 2$) with the emission of two electrons but no
⁶ (anti-)neutrinos.

⁷ The CUORICINO experiment was a ^{130}Te -based search for $0\nu\beta\beta$. It consisted of
⁸ an array of 62 tellurium dioxide (TeO_2) bolometers with a total mass of 40.7 kg. It
⁹ was operated at the Laboratori Nazionali del Gran Sasso (LNGS) in Assergi, Italy,
¹⁰ from early 2003 to June 2008. The CUORICINO detector was built as a prototype
¹¹ for the CUORE experiment, which will have 19 CUORICINO-like towers and is
¹² presently under construction at LNGS.

¹³ The CUORICINO crystals were arranged in a tower made of 13 levels, 11 with
¹⁴ four $5 \times 5 \times 5 \text{ cm}^3$ crystals and 2 with nine $3 \times 3 \times 6 \text{ cm}^3$ crystals. Each crystal was
¹⁵ operated as a bolometer able to detect an energy deposition by recording the resulting
¹⁶ temperature increase with a neutron transmutation doped Ge thermistor [1]. In the
¹⁷ case of $0\nu\beta\beta$, the summed energies of the electrons and recoiling nucleus would result
¹⁸ in a mono-energetic peak at the $0\nu\beta\beta$ transition energy of $2527.518 \pm 0.013 \text{ keV}$ for
¹⁹ ^{130}Te [2].

²⁰ The detector operated at $\sim 10 \text{ mK}$, cooled by a dilution refrigerator and sur-
²¹ rounded by several layers of shielding. Directly above the detector was a 10 cm thick
²² layer of low-activity “Roman” lead (from ancient Roman shipwrecks). Around the
²³ sides of the detector were several layers of thermal shields and a 1.2 cm thick cylindri-
²⁴ cal Roman lead shield. The thermal shields were made from electrolytic copper and
²⁵ totaled at least 1.5 cm in thickness. Outside the cryostat was a 10 cm low-activity
²⁶ lead shield and a 10 cm standard lead shield. The cryostat and shields were sur-
²⁷ rounded by a Plexiglas box flushed with clean N_2 from a liquid nitrogen evaporator
²⁸ to avoid radon, followed by a 10 cm borated polyethylene neutron shield. A top lead

29 shield was located about 50 cm above the top plate of the cryostat. The entire setup
 30 was enclosed in a Faraday cage to reduce electromagnetic interference. The assembly
 31 is shown in Figure 1. A more detailed description of the detector can be found in
 32 Ref. [1].

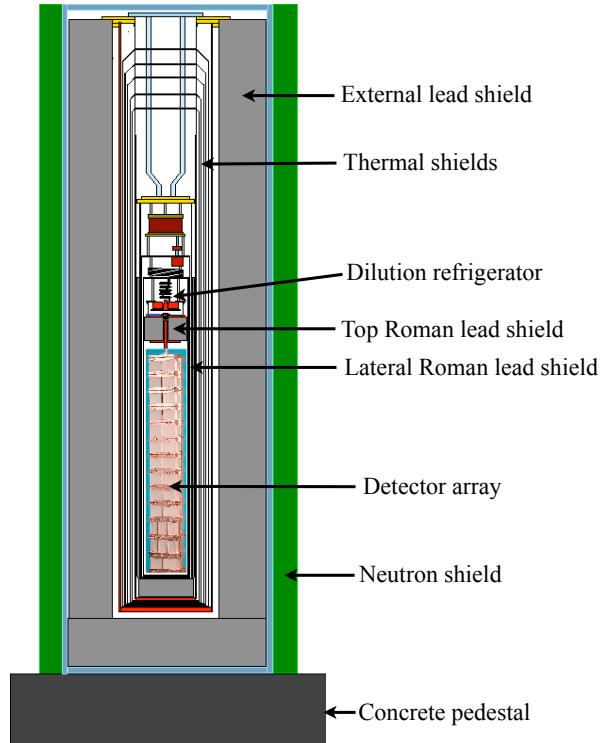


Figure 1: The layout of CUORICINO showing the tower, the various heat shields, and the external shielding

33 In CUORICINO, any single-bolometer energy deposition in the $0\nu\beta\beta$ energy re-
 34 gion is a potential background that can decrease the sensitivity of the experiment.
 35 Cosmic rays are one source of background. The 3200 mwe overburden at Gran Sasso
 36 eliminates the soft cosmic ray component and reduces the flux of penetrating muons
 37 by six orders of magnitude to $\sim 1.1 \mu/(h \cdot m^2)$ [3], with a mean energy of ~ 270 GeV
 38 and an average zenith angle $\langle\theta\rangle \sim 35$ degrees. The azimuthal distribution reflects
 39 the mountain profile [4, 5].

40 A muon could produce a bolometer signal by interacting directly in the detector.
 41 Additionally, muons interacting in the detector, shieldings, or surrounding materials

42 could create secondary products that might mimic a $0\nu\beta\beta$ decay. For example,
 43 neutrons produced by cosmic rays are very energetic and thus difficult to block
 44 with shields. Photons emitted in $(n, n'\gamma)$ or (n, γ) reactions could appear near the
 45 $0\nu\beta\beta$ energy. Neutron production increases with the atomic weight of the material;
 46 therefore, lead shields can be a strong source of muon-produced neutrons. However,
 47 neutron production is mostly associated with showers, so this background may be
 48 effectively identified by coincident events in different bolometers.

49 Several Monte Carlo simulations have been carried out on cosmic ray-induced
 50 backgrounds but few direct measurements have been made [6, 7, 8, 9, 10, 11, 12, 13,
 51 14]. For the present study, an external muon detector was installed to tag muon-
 52 induced background events in CUORICINO during its last three months of operation.

53 Section 2 and Section 3 give details of the muon detector setup and performances.
 54 Section 4 is a summary of the Monte Carlo simulations, while Section 5 describes
 55 the data analysis and results.

56 2. Muon Detector Setup

57 An array of ten large plastic scintillators placed outside of the Faraday cage,
 58 which surrounds the detector, was used to tag muons. The scintillation counters
 59 were obtained from previous experiments; the various types are described in Table 1.
 60 The total sensitive surface area of the scintillators was about 3.67 m^2 . A photograph
 61 of four of the scintillators is shown in Figure 2.

Scintillator Label	Length (cm)	Width (cm)	Thickness (cm)	Number of PMTs
A1	100	50	5	1
A2	100	50	5	1
B1	120	60	15	2
B2	120	60	15	2
C1	96	42.5	3.2	1
C2	55	64	3.2	1
D1	200	20	3	1
D2	200	20	3	1
D3	200	20	3	1
D4	200	20	3	1

Table 1: Dimensions of the plastic scintillators used

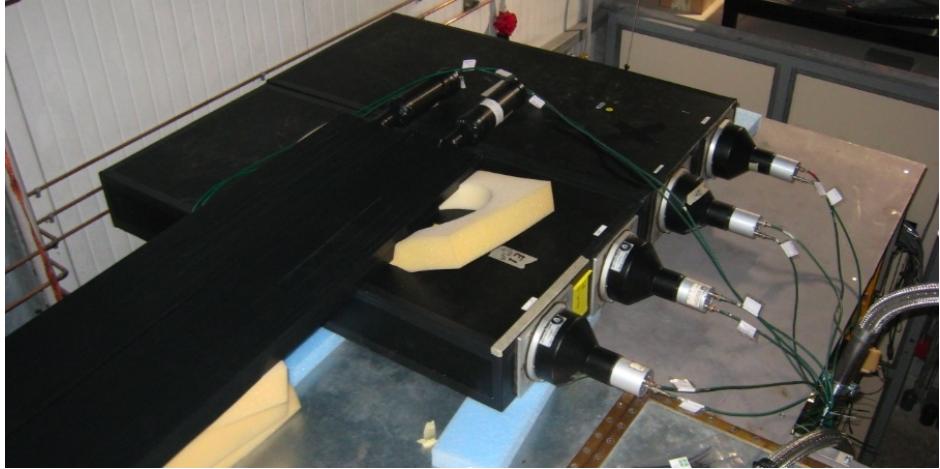


Figure 2: Four of the ten scintillators used (types B and D), shown from the top of the CUORICINO Faraday cage

62 The scintillators were deployed to tag as many as possible of the muons hitting
 63 the lead shields while accounting for both the angular distribution of the incoming
 64 muons and the geometric constraints from existing structures. A simple Monte Carlo
 65 simulation reproducing the muon flux measured by MACRO [5] was used to optimize
 66 the placement of the counters. The arrangement of the scintillators is shown in Figure
 67 3.

68 Each scintillator was read out by one photomultiplier tube (PMT) attached to
 69 one of its smallest faces, except the type B scintillators which had two PMTs on the
 70 same face with their outputs summed.

71 The type A and B scintillators were the thickest and were operated alone. For
 72 these scintillators, the energy released by a through-going minimum ionizing particle
 73 was greater than 8 MeV, which was well above any naturally occurring gamma or
 74 beta background as well as most naturally occurring alpha lines; therefore, muons
 75 may be discriminated from background by simply applying cuts on the energy. The
 76 type C and D scintillators were about 3 cm thick and were operated in pairs. For
 77 each pair, one scintillator was stacked on top of the other and a trigger signal was
 78 generated only when they were hit in coincidence (within 120 ns of each other), as
 79 indicated in Figure 4. A 5 cm thick layer of lead was placed between each pair of
 80 type D scintillators to further reduce backgrounds.

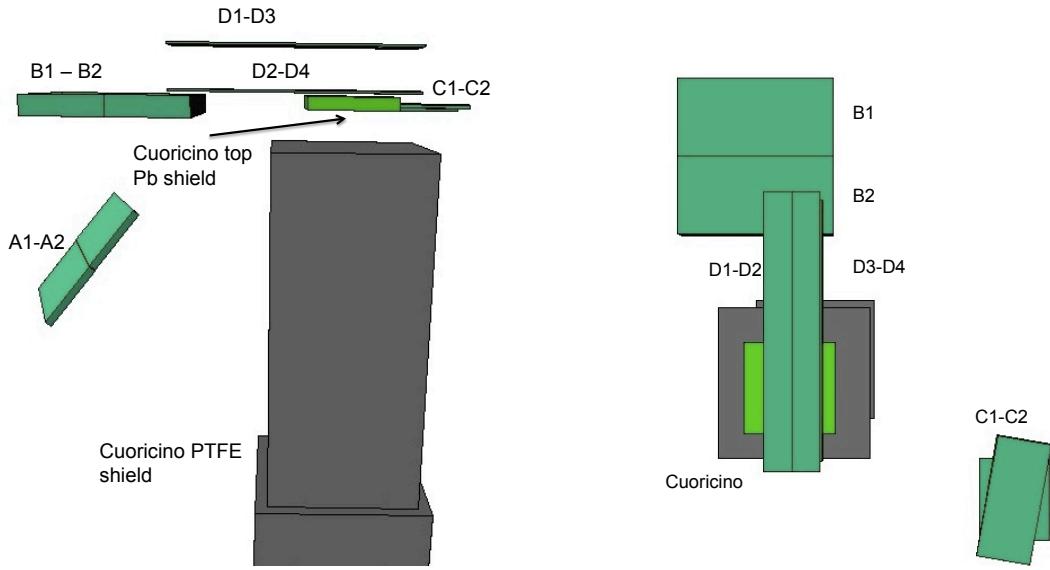


Figure 3: The drawings show the positions of the scintillators around CUORICINO (left: side view, right: top view): the large, dark grey box is the neutron shield placed around the detector, and the smaller objects are the scintillators and the top part of the lead shield. The support structures for the scintillators have been omitted.

81 The signals from the PMTs were sent to the electronics and data acquisition
 82 (DAQ) systems. The analog electronics stage, constructed from commercial NIM
 83 modules, was responsible for generating the trigger signals; the analog signals were
 84 afterwards digitized by a dedicated VME data acquisition system synchronized with
 85 the CUORICINO DAQ (Figure 4). Each PMT signal was split in two copies: one
 86 was sent to a threshold discriminator; the other, after being delayed, was fed into
 87 a VME QDC board (Caen V792 N). The QDC board recorded the charge from the
 88 PMT (integrated over 120 ns), which was proportional to the energy released in the
 89 scintillator. The logic signals from the threshold discriminators were also split: one
 90 copy went to the NIM boards implementing the trigger logic, while the other went
 91 to a VME TDC board (Caen V775 N). The TDC board recorded the relative time
 92 between all PMT signals and the trigger, with a nominal precision of 70 ps. However,
 93 since the typical time resolution of the PMTs was 1–2 ns, the relative time between
 94 multiple PMT hits associated with a single trigger is known to a few ns, while the
 95 absolute trigger time is known only to the precision of the CUORICINO DAQ (8
 96 ms).

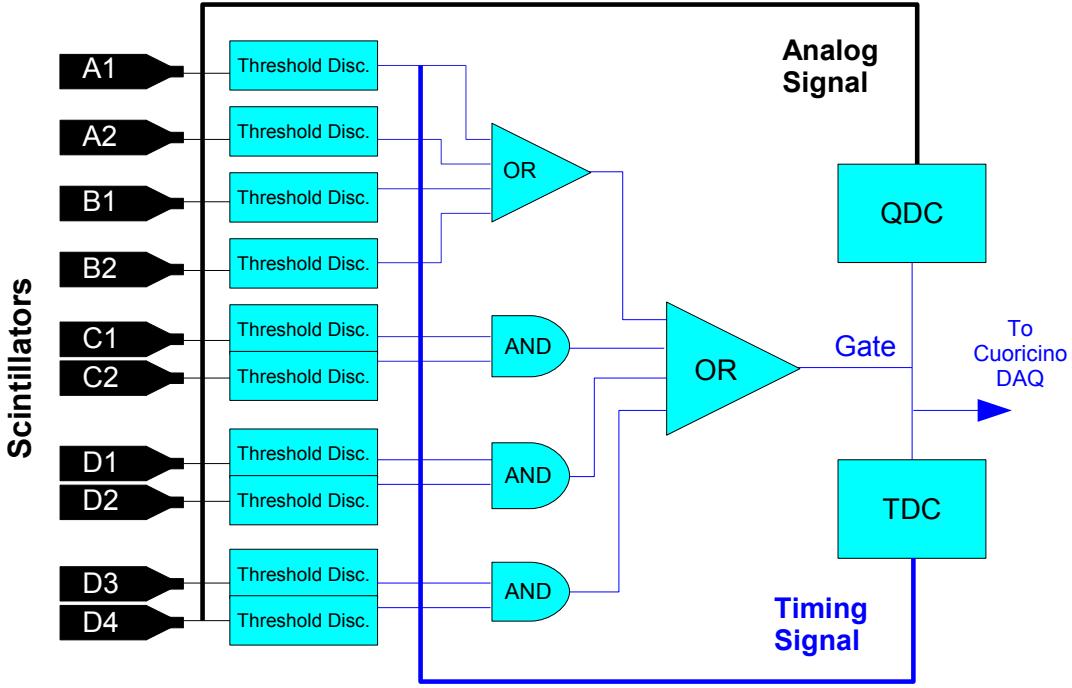


Figure 4: Principle of operation of the electronics and the DAQ system

97 3. Detector Operation and Performance

98 The muon tagging system was operated with CUORICINO from 12 March to
 99 26 May 2008. The system was running $\sim 53\%$ of the time because of CUORICINO
 100 calibrations and downtime for repairs and maintenance; the total live time was 38.6
 101 days.

102 Figure 5 shows the energy spectrum acquired by one of the type A scintillators.
 103 Two regions are evident: a low energy background region and a broad peak at higher
 104 energies. The low energy background is due to radioactivity, dark noise, and muons
 105 that clip the scintillator, whereas the higher energy peak is mostly due to cosmic ray
 106 muons.

107 The efficiencies of the detectors were measured above ground in the assembly
 108 hall of LNGS, where the muon rate was much larger. The measurement was made
 109 by placing a pair of scintillators (A and B) above and below the scintillator whose
 110 efficiency was being measured (C), such that any muon passing through both A and

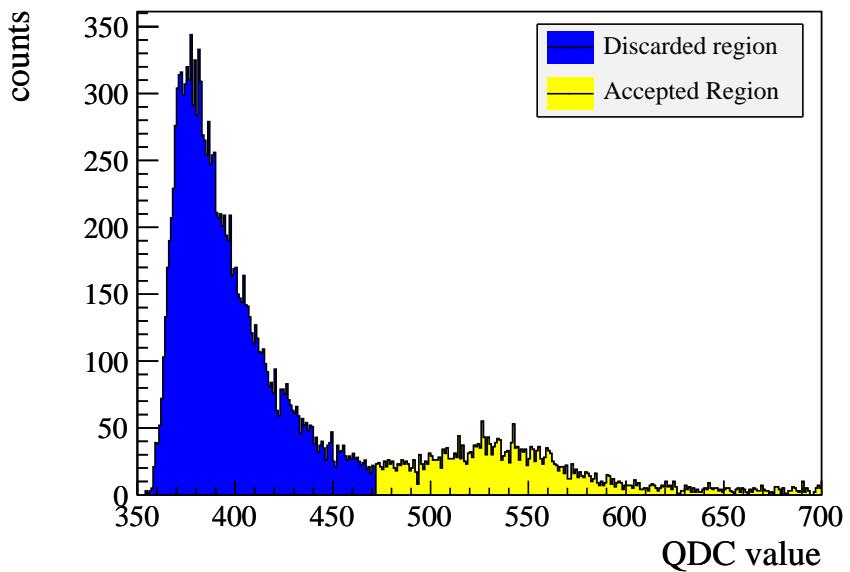


Figure 5: Energy spectrum acquired underground at LNGS using detector A1. The darker region (not used in the analysis) is dominated by low energy background, while lighter region primarily contains muon events. The X axis is QDC counts, proportional to energy.

111 B must also pass through C. If N_{AB} is the number of hits occurring in coincidence
112 in detectors A and B, and N_{ABC} is the number of hits in coincidence between all 3
113 detectors then the efficiency of detector C is simply $\eta_C = N_{ABC}/N_{AB}$. Of course, the
114 efficiency depends on the thresholds set by the threshold discriminators; the thresh-
115 olds were chosen based on these measurements to be as high as possible while still
116 maintaining an efficiency close to unity. The individual efficiencies of the detectors
117 measured in this fashion were generally greater than 95%; however, there was an
118 additional loss of efficiency from cuts applied in the analysis to reduce background
119 (described below).

120 Muons were discriminated from the background in the thick scintillators (types
121 A and B) with an energy cut: for these detectors a software threshold was set at
122 the dip between the signal and background regions in the spectrum (Figure 5). A
123 rough estimate of the loss of efficiency due to this cut was obtained by assuming
124 a Gaussian shape for the muon peak. For the type A (5 cm thick) detector shown
125 in Figure 5, this cut rejected $\sim 10\%$ of the muons, although for the thicker type B
126 (15 cm) detectors, the estimated loss of efficiency was less than 1%.

127 For the thin scintillators, coincidences between different detectors were used to
128 generate triggers as described in Section 2 and no further cut on the energy of the
129 events was applied in the analysis, since the muon peak was not well separated from
130 the background in the energy spectrum.

131 In order to determine the overall efficiency of the setup for tagging muons asso-
132 ciated with CUORICINO bolometer events, the intrinsic detector efficiency and the
133 efficiency of the software cuts were combined for each detector. This information was
134 then included in a Monte Carlo simulation precisely reproducing the CUORICINO
135 geometry, the positions of the scintillators, and the distribution of the muon flux.
136 The simulation is described in more detail in Section 4.

137 The total trigger rate of the muon detectors combined was ~ 14 mHz with no cuts
138 applied, or ~ 4 mHz with energy threshold cuts, while the expected signal rate from
139 the simulation was 1.75 mHz. The difference between the predicted and measured
140 rate is due to the fact that the trigger thresholds were kept low in order to maximize
141 the efficiency of muon detection; this resulted in the inclusion of some triggers caused
142 by radioactive decays and dark noise. These spurious muon triggers contributed some
143 background to our measurement through the increased rate of accidental coincidences
144 between the scintillators and bolometers, which was taken into account in the analysis
145 described in Section 5.

146 **4. Simulation**

147 GEANT4 version 9.2¹ [15] was used to simulate the muon-induced backgrounds in
148 CUORICINO. The LBE (Low Background Experiment) physics list was used. The
149 GEANT4 capability of event-by-event simulation was employed to follow the whole
150 sequence of secondary tracks from the initial interaction to the detector, including
151 the contribution of neutrons generated from muon interactions in the shields. The
152 complete structure of the scintillators, external shields, internal shields, and detector
153 geometry was implemented according to the model shown in Figure 3. The propagation
154 of particles through the rock overburden was not simulated, but was accounted
155 for as described below.

156 An external code simulated the muon energy and angular distribution in the
157 underground laboratory of LNGS. Muons were generated on a 6 m hemisphere in
158 the underground laboratory according to the angular distribution measured by the
159 MACRO experiment [5]. The generated muons were then assigned an energy based
160 on the ground-level energy spectrum for that angle, which was approximated as [16]:

$$\frac{dN}{dE_{GL} \cdot d\Omega} \propto \frac{0.14 \cdot E_{GL}^{-2.7}}{\text{s cm}^2 \text{ sr GeV}} \left(\frac{1}{1 + \alpha E_{GL} \cos \theta} + \frac{0.054}{1 + \beta E_{GL} \cos \theta} \right), \quad (1)$$

161 where E_{GL} is the energy at ground level, $\alpha = 1.1/115$ GeV, and $\beta = 1.1/850$ GeV.
162 The ground-level energy was then translated into an underground energy based on
163 the formula [16]:

$$E_U = (E_{GL} + \epsilon) \cdot e^{-bX(\theta, \phi)} - \epsilon, \quad (2)$$

164 where E_U is the energy underground, $b = 0.4 \times 10^{-5} \text{ cm}^2/\text{g}$, $\epsilon = 540.0$ GeV, and
165 $X(\theta, \phi)$ is the thickness times density of the overburden in the given direction. The
166 advantage of this method is that it includes the correlation between the direction and
167 energy of the muons underground. The range of above-ground energies simulated was
168 chosen for each direction such that the underground energies spanned from 1 GeV
169 to 2 TeV, which corresponds to $\sim 99\%$ of the underground muon flux.

170 The output of the simulation contained the event number, detector number (scin-
171 tillator number or bolometer number), hit time, and energy released in the detector.
172 This output was used to produce spectra and scatter plots, taking into account the
173 detector response and analysis cuts in order to reproduce the experimental condi-
174 tions. A Gaussian smearing of 8 keV (full-width at half maximum) modeled the
175 bolometer resolution.

¹A known bug affecting the neutron inelastic interactions has been fixed in GEANT4 9.2:
<http://geant4.cern.ch/support/ReleaseNotes4.9.2.html>

176 The Monte Carlo simulation produced the equivalent of about 3.5 years of data
177 ($\sim 8 \times 10^6$ primary muons). In addition to statistics, the simulations were subject
178 to systematic uncertainties: uncertainty in the primary muon flux and spectrum
179 (8%) [3], GEANT4 electromagnetic tracking (5%), uncertainty in the muon-induced
180 neutron yield (40%), and neutron propagation and interaction (20%) [17]. Analysis
181 of simulation results will be discussed in Section 5.1.

182 **5. Data Analysis**

183 The analysis involved searching for correlations between muon triggers and events
184 in the CUORICINO bolometer array. A coincidence was defined as a muon detector
185 event occurring within ± 50 ms of a bolometer event. This large window, chosen
186 based on the time resolution of the bolometer signals (~ 30 ms), was not a limitation
187 due to the low event rates.

188 The bolometer spectrum was divided into three energy regions: 200–400 keV,
189 400–2000 keV, and 2000–4000 keV, as shown in Figure 6. The background rate varies
190 by several orders of magnitude over the complete spectrum; therefore, it is useful to
191 treat the high energy region, which contains the Q-value for $0\nu\beta\beta$ decay ($2527.518 \pm$
192 0.013 keV), separately from the lower energy regions where the background is much
193 higher. In addition to the $0\nu\beta\beta$ Q-value, the high energy region contains the ^{208}Tl
194 γ line at 2614.5 keV, the ^{190}Pt α line at 3249 keV (including nuclear recoil), and
195 an approximately constant background from 3–4 MeV, which is believed to be due
196 to degraded alphas. This region may also have a cosmic ray component, and was
197 therefore investigated with this measurement.

198 In the limit of low rates, the rate of “accidental” coincidences between muon
199 events and bolometer events is given by:

$$R_{\text{accidental}} = 2 \cdot R_{\text{bolo}} \cdot R_\mu \cdot \Delta T \quad (3)$$

200 where R_{bolo} is the bolometer event rate, $R_\mu = 4.01$ mHz is the muon rate, and $\Delta T = 50$
201 ms is the width of the coincidence window. Multiplying this rate by the total live
202 time gives the expected number of accidental coincidences, which is compared to the
203 number of measured coincidences in Figure 7(a). This figure shows a statistically
204 significant correlation between events in the muon detector and the bolometers.

205 The usual CUORICINO $0\nu\beta\beta$ analysis includes an anti-coincidence cut which
206 excludes any bolometer event that occurs within 100 ms of any other bolometer
207 event. The bolometer anti-coincidence condition is used to reduce background, since
208 the $0\nu\beta\beta$ signal is expected to appear only in one bolometer. Limiting the analysis to
209 single-bolometer events, the number of coincidences between the muon and bolometer

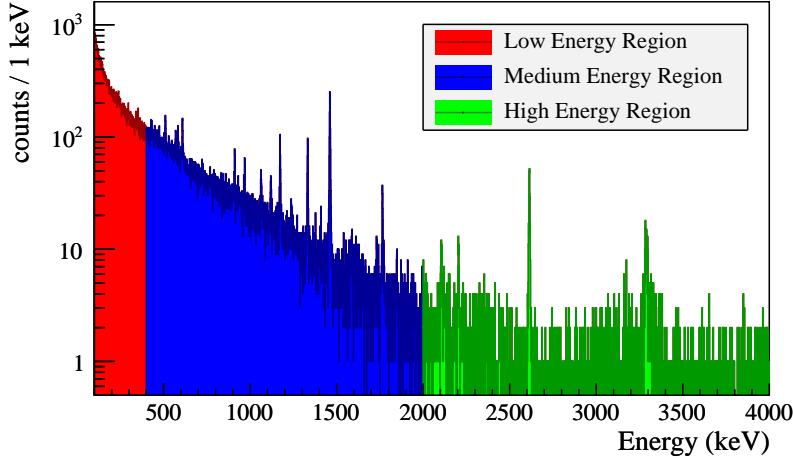


Figure 6: Energy spectrum of the CUORICINO background showing the division of energy regions used in the analysis. No bolometer anti-coincidence cut has been applied.

events is consistent with the number of expected accidentals, as shown in Figure 7(b). Evidently, the bolometer anti-coincidence cut is very effective at eliminating potential muon-induced backgrounds.

The numbers of expected accidental and measured coincidences shown in Figure 7(b) provide an upper limit on the muon-induced contribution to the CUORICINO background. These results are summarized in Table 2. The limits were computed by using the Feldman-Cousins method [18] to obtain an upper limit, ν^{up} , on the expected number of muon-correlated signal events. This number was converted into an upper limit on the background rate, R^{up} , in the usual units of counts/(keV·kg·yr) as follows:

$$R^{\text{up}} = \nu^{\text{up}} \cdot \frac{1}{f_{\text{obs}}} \cdot \frac{1}{X} \cdot \frac{1}{\Delta E} \quad (4)$$

Here, $X = 3.99 \text{ kg}\cdot\text{yr}$ is the total exposure (active bolometer mass times live time) and ΔE is the size of the energy window. The error on the energy window is taken to be on the order of the energy resolution, 7–9 keV on average. The factor $f_{\text{obs}} = 13.6 \pm 1.6\%$ is the fraction of the muons producing signal in bolometers that are also observed in the scintillators. It is obtained from the simulation described in Section 4 by taking the number of muon events which hit the bolometers *and* the scintillators divided by the total number of generated muon events which hit the

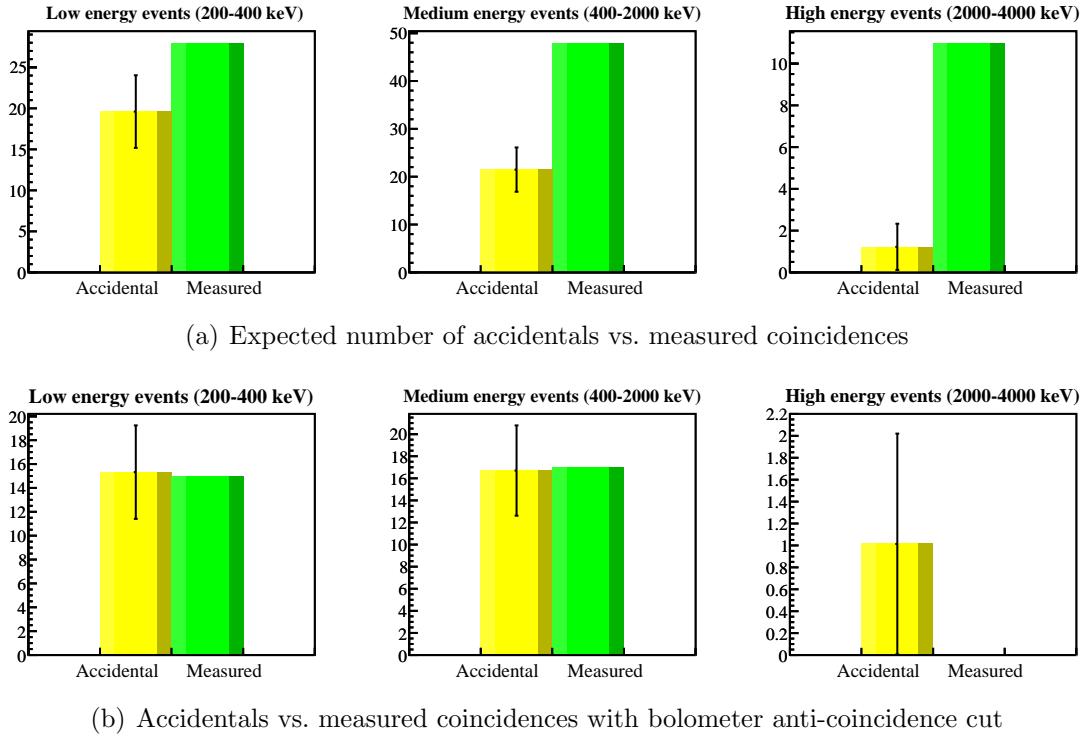


Figure 7: Comparison of the expected number of accidental coincidences and the number of observed coincidences between the muon detector and bolometer signals. The error bar on the accidentals column represents Poisson fluctuations. Figure 7(a) includes all bolometer events in the given energy region, while Figure 7(b) only includes bolometer events which pass an anti-coincidence cut (i.e. they do not occur within 100 ms of any other bolometer event).

Energy	$\langle A \rangle$	M	Upper Limits (95% CL)	
			ν^{up}	$R^{\text{up}}/10^{-3}$
Low (200-400 keV)	15.3	15	9.0	83
Mid (400-2000 keV)	16.7	17	10.	12
High (2-4 MeV)	1.01	0	2.3	2.1

Table 2: Upper Limits (95% CL) on the contribution of muon-induced events to the CUORICINO background. Limits were computed using the Feldman-Cousins method. $\langle A \rangle$ is the expectation value of the number of accidental coincidences. M is the number of measured coincidences. ν^{up} is a limit on the mean number of observed muon-correlated signal events, while R^{up} gives an upper limit on the rate in counts/(keV·kg·yr).

227 bolometers. The uncertainty in f_{obs} is the dominant systematic uncertainty in the
 228 conversion from ν^{up} to R^{up} ; however, this uncertainty is much smaller than the
 229 statistical uncertainty, and has therefore been neglected in computing upper limits.
 230 After applying the bolometer anti-coincidence cut, the upper limit on the muon-
 231 induced contribution to the CUORICINO background in the $0\nu\beta\beta$ region of interest
 232 is 0.0021 counts/(keV·kg·yr) at 95% confidence level.

233 In principle, a muon (or spallation neutron) could produce long-lived ($T_{1/2} \gtrsim 50$
 234 ms) radioactive isotopes which could then decay producing a delayed coincidence
 235 signal. Based on the small number of muon events and large background, we do not
 236 expect to be sensitive to this effect. Consistent with this expectation, we find no
 237 evidence of a delayed coincidence signal. However, due to the poor sensitivity and
 238 large number of potential products (each with a different half-life and decay energy),
 239 we do not set an upper limit for delayed coincidences with the present data.

240 *5.1. Simulation Results*

241 The analysis of the simulated events was carried out in the same way as for
 242 the actual measurements. The spectrum of muon events in the various scintillators
 243 appears to be correctly reproduced in simulations. The spectrum of bolometer events
 244 was divided into the same three energy regions: 200–400 keV, 400–2000 keV, and
 245 2000–4000 keV.

246 In Table 3, the simulated rates of bolometer events in coincidence with the muon
 247 detector are reported and compared with data (with and without imposing a bolome-
 248 ter anti-coincidence cut). The measured rates are reported after the subtraction of
 249 the expected background from accidental coincidences. In Table 4, the simulation
 250 results are reported for the total muon-induced background rate in CUORICINO. In

	Simulation 10^{-3} (counts/(keV·kg·yr))	Measurement 10^{-3} (counts/(keV·kg·yr))
All Events		
Low (200-400 keV)	25.0 ± 0.7	10 ± 7
Mid (400-2000 keV)	7.91 ± 0.14	4.2 ± 1.1
High (2-4 MeV)	1.71 ± 0.12	1.2 ± 0.4
With Bolometer Anti-coincidence Cut		
Low (200-400 keV)	1.84 ± 0.19	< 11
Mid (400-2000 keV)	0.66 ± 0.04	< 1.6
High (2-4 MeV)	0.08 ± 0.03	< 0.29

Table 3: Simulated and measured rates of bolometer events in coincidence with the muon detector. Only statistical errors are quoted. Systematic uncertainties are discussed in the text (Sections 4 and 5).

Energy	Total 10^{-3} (counts/(keV·kg·yr))	Anti-coincidence 10^{-3} (counts/(keV·kg·yr))
Low (200-400 keV)	184.9 ± 1.9	7.9 ± 0.4
Mid (400-2000 keV)	58.1 ± 0.4	3.58 ± 0.09
High (2-4 MeV)	12.6 ± 0.3	0.53 ± 0.06

Table 4: Simulated contribution of muon-induced events to the CUORICINO background. Only statistical errors are quoted. Systematic uncertainties are discussed in the text (Section 4).

251 the energy region immediately surrounding the $0\nu\beta\beta$ Q-value (2507.5–2547.5 keV),
252 a value of $(17.4 \pm 1.3) \times 10^{-3}$ counts/(keV·kg·yr) was obtained for background in-
253 duced by muons without any anti-coincidence cut applied and a value of $(0.61 \pm$
254 $0.25) \times 10^{-3}$ counts/(keV·kg·yr) with the bolometer anti-coincidence cut.

255 6. Conclusions

256 The bolometer anti-coincidence cut in CUORICINO appears to be a very effective
257 tool for eliminating muon-induced backgrounds. With this cut, the measured rate
258 of muon-correlated, single-bolometer background events was consistent with zero,
259 and an upper limit of 0.0021 counts/(keV·kg·yr) (95% C.L.) in the $0\nu\beta\beta$ region of
260 interest was obtained.

261 The results of the measurement have been compared with a detailed GEANT4
262 simulation. Although the sensitivity of the experiment was not sufficient to perform
263 a rigorous validation, the results of the measurement and simulation were generally
264 compatible.

265 The rate obtained for the muon-induced contribution to the CUORICINO back-
266 ground, by measurement or simulation, is small compared to the total CUORICINO
267 background rate of ~ 0.2 counts/(keV·kg·yr) in the region of interest. Muon interac-
268 tions also do not appear to contribute significantly to the background rate between
269 3–4 MeV.

270 The muon-induced backgrounds may not scale directly from CUORICINO to
271 CUORE because of differences in the detector and shield geometry, materials, and
272 anti-coincidence efficiency. For that reason, a detailed simulation, similar to that
273 described in Section 4, has also been performed for muons and other external back-
274 grounds in CUORE [19]. However, omitting subtle changes, the muon-induced back-
275 ground rates in CUORE should be of a similar order of magnitude to those obtained
276 for CUORICINO. The CUORE goal for the total background rate in the region of
277 interest is 0.01 counts/(keV·kg·yr), and both the measured and simulated values for
278 the muon-induced background in CUORICINO are well below the CUORE goal.

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